

Post Graduate Problem Set 1

To be handed in to PTD before the tutorial on November 9, 2006

1. The LEP1 collider at CERN collided electrons with positrons, both with energy 45 GeV. What positron beam energy would be required to obtain the same centre-of-mass energy on a stationary electron target? The proposed LHC will collide protons with protons at a beam energy of 7 TeV. What beam energy would be required for the same centre-of-mass energy in a fixed target experiment in this case?



2. The π^0 is a spinless particle of mass 135 MeV which decays electromagnetically to two photons, $\pi^0 \rightarrow \gamma\gamma$, with a lifetime of 8.4×10^{-17} s. Show that the laboratory photon energy spectrum from pions is flat and compute its boundaries, E_γ^{\min} and E_γ^{\max} . Sketch the spectrum for pions with total lab energy:
a) 135 MeV; **b)** 500 MeV; **c)** 1 GeV.



3a) Use the Fermi Golden Rule to derive an expression for the differential cross-section, $d\sigma/d\Omega$, for two-particle scattering ($A+B \rightarrow C+D$; $m_A=m_B$) in the centre-of-mass frame, in terms of the matrix element \mathcal{M} . **b)** If the particles are pointlike (*i.e.* zero size), how should the cross section vary as a function of energy?



4. The ratio of the total cross-section for e^+e^- annihilation into hadrons to the $e^+e^- \rightarrow \mu^+\mu^-$ cross-section is called R. **a)** Derive a formula for R between threshold and $E_{CM} > 2m_b$, where m_b is the b-quark mass. **b)** List the processes which contribute to the variation of R between threshold and 200 GeV centre-of-mass energy.



5. The η is a spinless particle of mass 547 MeV which (like the π^0 , question 2 above) decays electromagnetically to two photons: $\eta \rightarrow \gamma\gamma$. **a)** Use the Fermi Golden Rule for decays to estimate the lifetime of the η , using the π^0 as an analogy. **b)** Given that the full width of the η is 1.2 keV and the branching ratio of its decay to two photons is 39%, discuss critically the assumptions made in your estimate.